Decomposition Guide Notes

Composition and Decomposition Defined

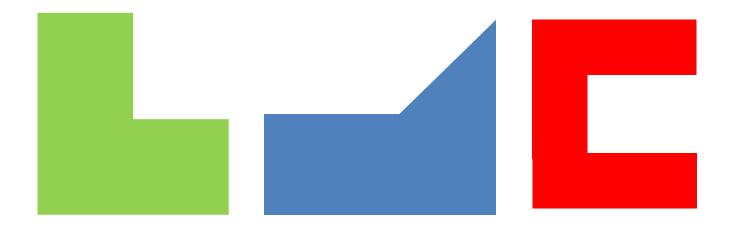
Composition and **Decomposition** came from the root word "compose" which means to join or put together. On the other hand, decomposition means to take apart or to separate.

In this lesson, decomposition will be used to find the area of irregularly-shaped polygons by separating them into triangles and/or other polygons.

The area of each separated part can then be added to find the area of the entire figure.

To determine the area of an irregularly-shaped polygon, the following have to be considered:

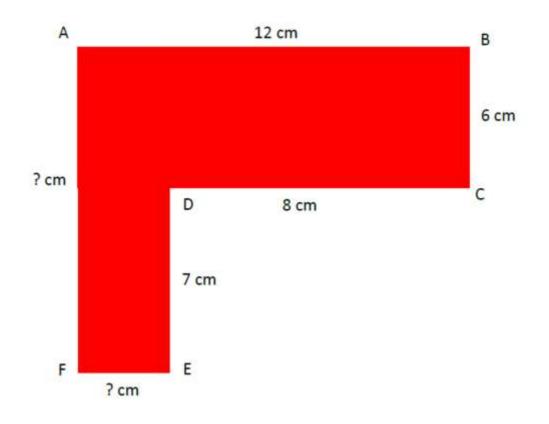
- + the skill in finding the length of the unknown sides
- **4** making decisions as to where to separate the figure to decompose irregularly-shaped polygons into rectangles and/or triangles



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Finding the Unknown Lengths

As mentioned, one very important skill needed in finding the area of an irregularly-shaped polygon is finding the lengths of any missing or unknown side. Consider the figure below:



How can the lengths of the missing sides be known?

In the example above, the lengths of sides AF and FE are unknown. To visually show the progression of the figures, vertical and/or horizontal lines will be drawn to separate the figure into rectangles.

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To find the missing length, we either add or subtract.

When do we add?

We add when the shorter sides are given (horizontal or vertical), to get the longer side.

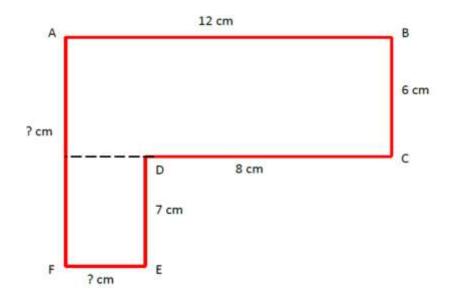
When do we subtract?

We subtract when one long side and one short side (horizontal or vertical) are given.

Decomposing Polygons into Rectangles

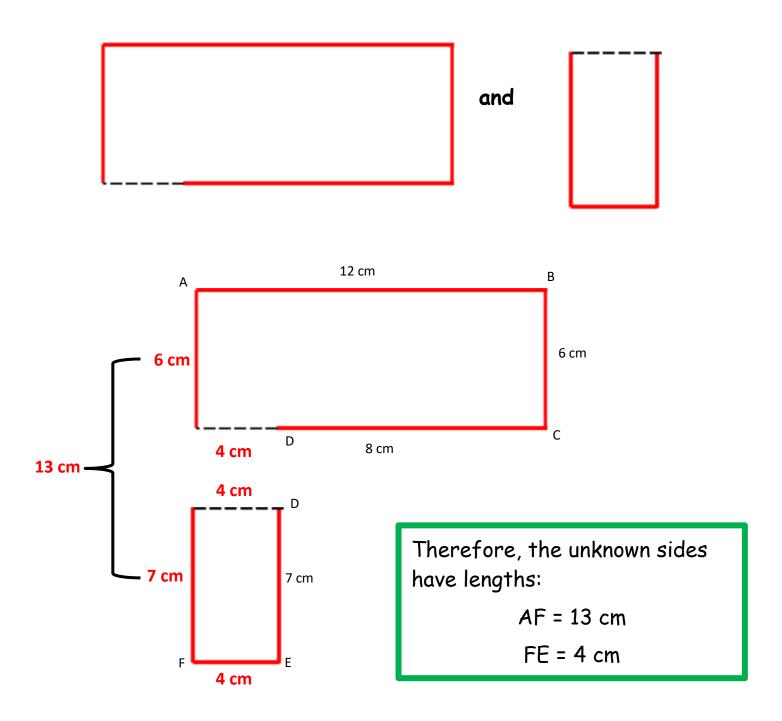
One's best judgment is used to decide how and where to separate an irregular polygon. Below is an example of the progression of figures.

Option A



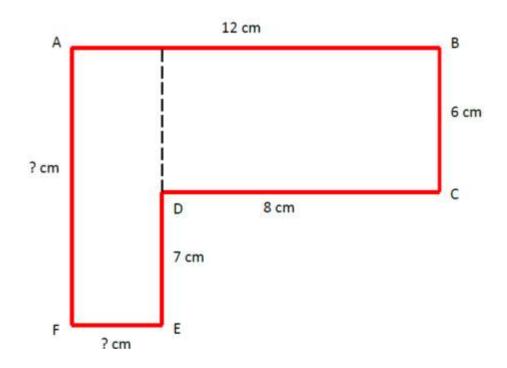
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Cutting the entire figure horizontally divides the figure into two separate rectangles.

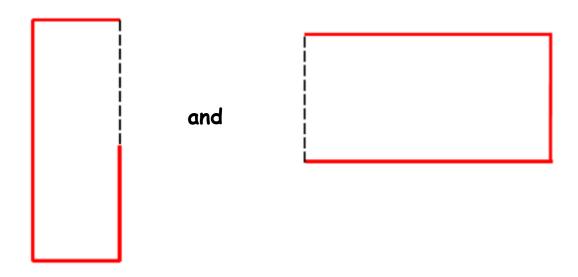


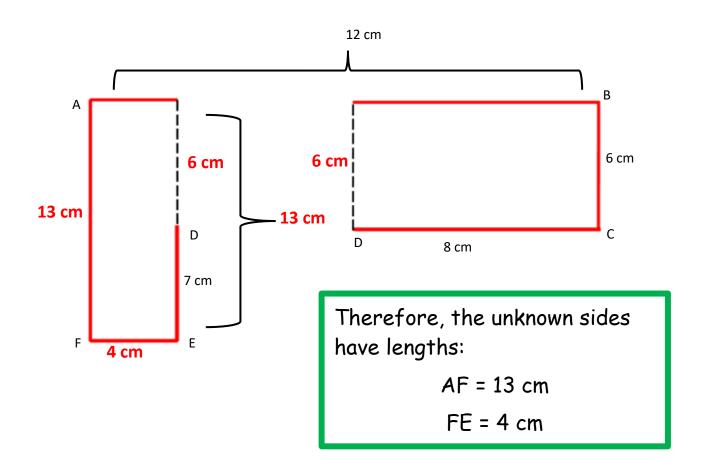
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Option B

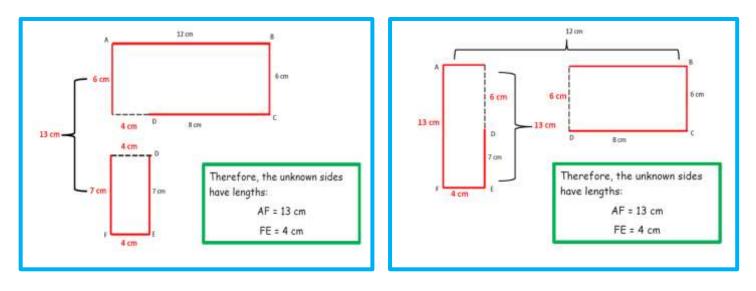


Cutting the entire figure vertically divides the figure into two separate rectangles.





The same values will come out whether the irregular polygons are separated into rectangles, horizontally or vertically.

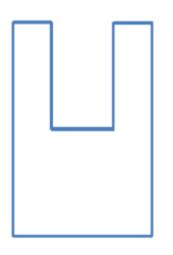


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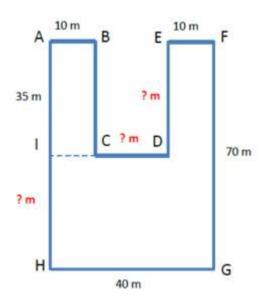
Sample Problem 1

Decompose the given figure into rectangles.



Sample Problem 2:

Find the missing lengths in the given figure.



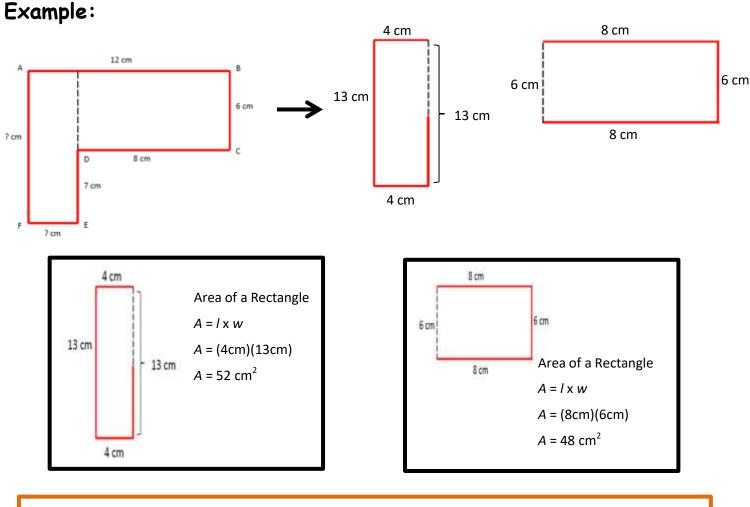
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The Area of Irregular Polygons

Steps to find the area of an irregularly-shaped polygon:

- **Step 1**: Decompose the irregularly-shaped polygon into rectangles.
- Step 2: Determine the length of any unknown side.
- Step 3: Solve for the area of each the decomposed rectangles.
- **Step 4:** Sum up all the area to get the area of the entire figure.

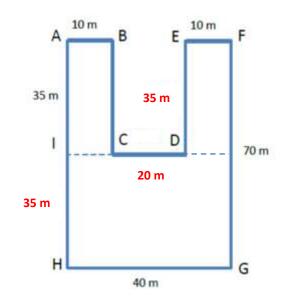


Total area of the figure = 52 cm² + 48 cm² = 100 cm^2

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Sample Problem 3:

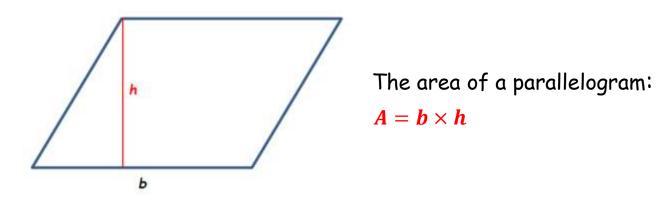
Find the area of the figure below.



Decomposing Polygons into Rectangles and Triangles

Decomposing Parallelograms

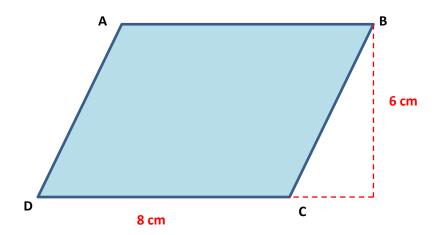
The area of a parallelogram can be determined by multiplying any of its base "b" to its corresponding altitude/height "h".



How can the area of a parallelogram be determined using only triangles?

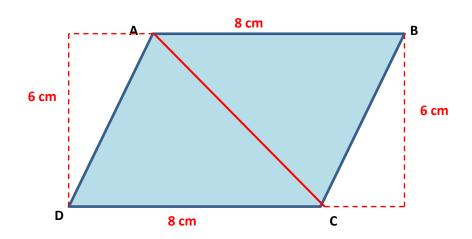
Example:

Below is parallelogram ABCD with base 8 cm and height 6 cm.



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Draw a diagonal from A to C, so 2 triangles are formed.



The 2 triangles formed are Triangle ABD and Triangle BCD. Find the area of the two triangles.

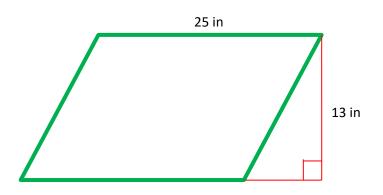
Area of Triangle ABC $A = \frac{1}{2}bh \text{ or } A = \frac{bh}{2}$ $A = \frac{(8)(6)}{2} = \frac{48}{2} = 24 \text{ cm}^2$ Area of Triangle ACD $A = \frac{1}{2}bh \text{ or } A = \frac{bh}{2}$ $A = \frac{(8)(6)}{2} = \frac{48}{2} = 24 \text{ cm}^2$

Area of Parallelogram ABCD = Area of Triangle ABD + Area of Triangle BCD Area of Parallelogram ABCD = 24 cm² + 24 cm² = 48 cm²

Since the two triangles are congruent, so as their areas. The area of a parallelogram can also be obtained by multiplying the area of one of the triangles by 2.

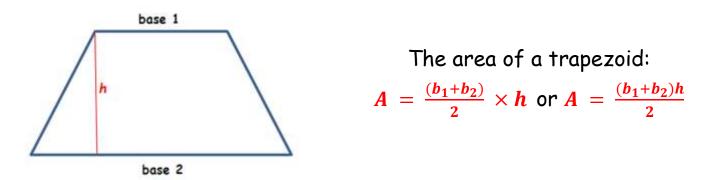
Sample Problem 4:

Find the area of the parallelogram below using triangles.



Decomposing Trapezoids

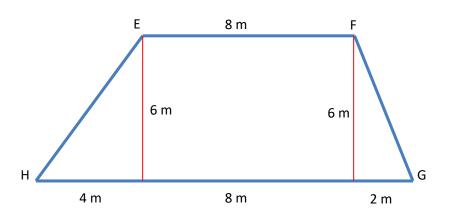
The area of a trapezoid can be determined by finding the average of the two bases and multiplying the answer by the given height.



Asiae from using the given formula, the area of trapezoids can be determined by composition and decomposition.

Example:

Below is Trapezoid EFGH with bases of lengths 8 m and 14 m respectively, with a height of 6m. Find its area.



Area of Triangle 1 $A = \frac{1}{2}bh \text{ or } A = \frac{bh}{2}$ $A = \frac{(4)(6)}{2} = \frac{24}{2} = 12 \text{ m}^2$

Area of Triangle 2 $A = \frac{1}{2}bh \text{ or } A = \frac{bh}{2}$ $A = \frac{(2)(6)}{2} = \frac{12}{2} = 6 \text{ m}^2$

Area of the Rectangle

$$A = lw$$

 $A = 8 \times 6 = 48 \text{ m}^2$

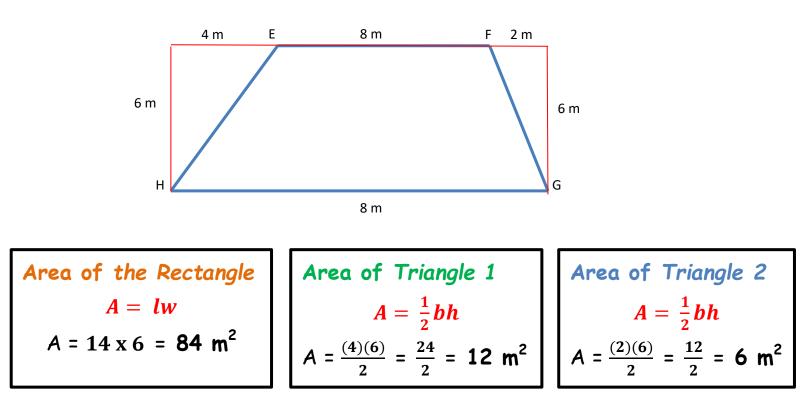
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Area of the trapezoid = Area of Triangle 1 + Area of Triangle 2 + Area of the Rectangle

Area of the trapezoid = $12 \text{ m}^2 + 6 \text{ m}^2 + 48 \text{ m}^2 = 66 \text{ m}^2$

But wait, there is another option:

If we surround the trapezoid with a rectangle, we can get its area by subtracting the area of the two triangles from the area of the rectangle.



Area of the trapezoid = Area of the Rectangle - (Area of Triangle 1 + Area of Triangle 2) Area of the trapezoid = 84 m^2 - (12 m^2 + 6 m^2) = 66 m^2 Notice that either way gives the same answer.

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Sample Problem 5:

Given the Trapezoid ABCD, find the following:

- a. CD = ?
- b. Area of Trapezoid ABCD

