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Multiplying Multi-Digit Whole Numbers

Unit 3 Lesson 2

Math 5

Students will be able to:

- I can multiply multi-digit whole numbers using area model and partial product.
- I can fluently multiply multi-digit whole numbers using standard algorithm.
- I can solve word problems involving multiplication of whole digit numbers.

Multiplying Multi-Digit Whole Numbers

Key Vocabulary:

Decomposing

Standard Algorithm

Multiplication

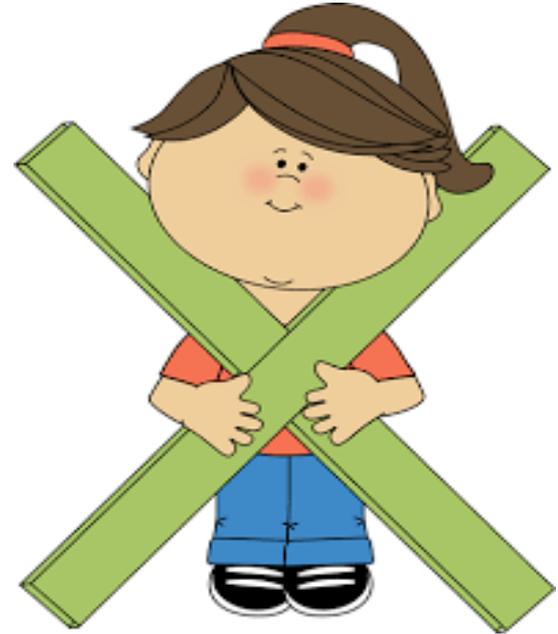
Place Value

Partial Product

Area Model

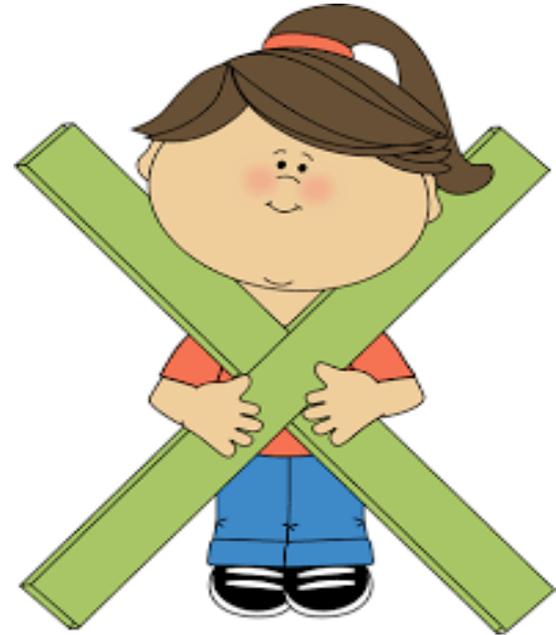
Multiplying Multi-Digit Whole Numbers

Just like **addition** and **subtraction**, **MULTIPLICATION** of multi-digit numbers has many strategies too! Drawing **area models**, **partial products** and using the **standard algorithm** are some of the many strategies used.



Multiplying Multi-Digit Whole Numbers

This lesson will enhance your fluency in multiplying multi-digit numbers using the "**standard algorithm**", but will also deal with the other two mentioned strategies.



Multiplying Multi-Digit Whole Numbers

Using Area Models to Multiply Multi-Digit Whole Numbers

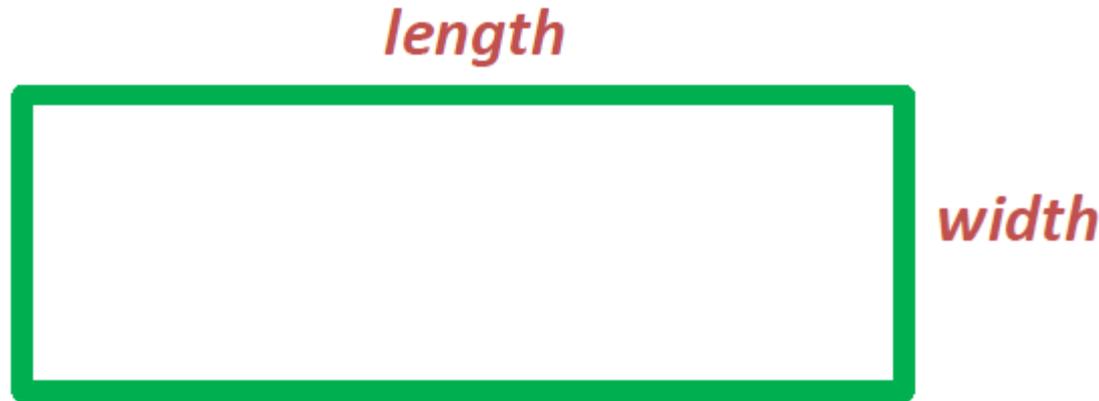
Area and **decomposing numbers** are the key concepts needed in multiplying multi-digit numbers using **area models**. The process involved may not be as easy and as fast as the standard algorithm, but this method provides a deeper mathematical understanding of the entire multiplication process.

How is it done?

Multiplying Multi-Digit Whole Numbers

Using Area Models to Multiply Multi-Digit Whole Numbers

Remember that each factor of any given multiplication problem is a dimension of a rectangle. These dimensions are the **length** and the **width**!



Multiplying Multi-Digit Whole Numbers

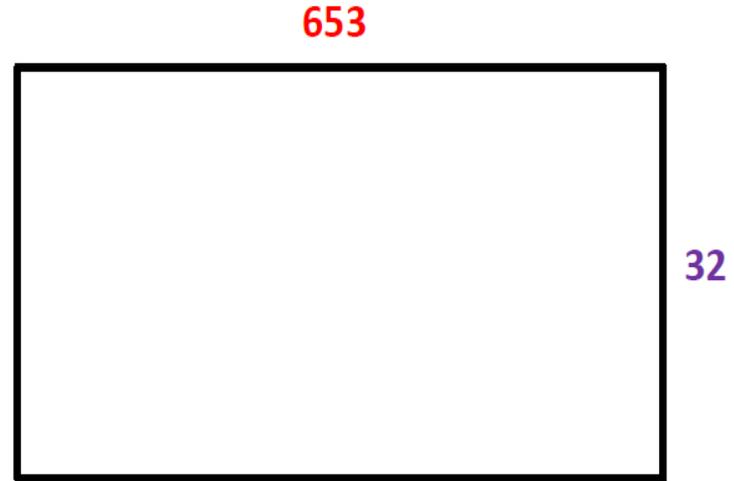
Example: Multiply 653 and 32 using area models.

Step 1: Draw a rectangle. The factors of the given multiplication problem will be the dimensions of the rectangle.

Let's say:

653 is the **Length**

32 is the **Width**



Multiplying Multi-Digit Whole Numbers

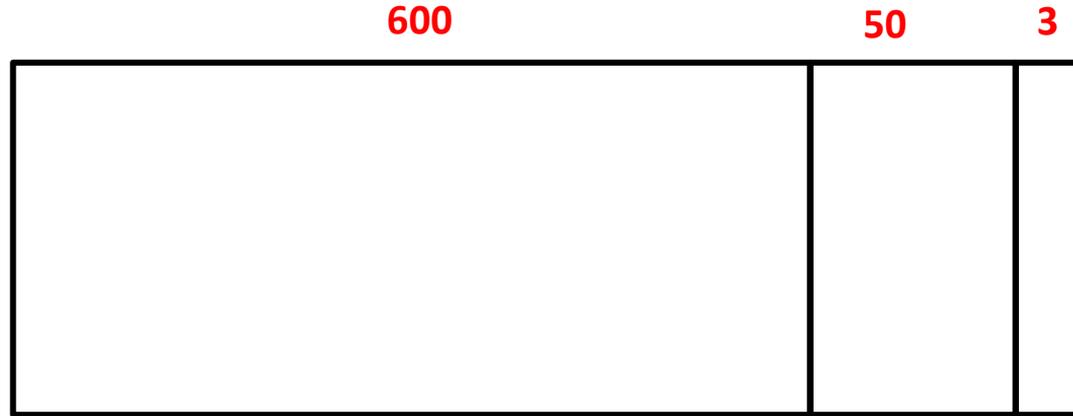
Step 2: Decompose the factors of the given multiplication problem using base ten numbers.

$$653 = 600 + 50 + 3$$

$$32 = 30 + 2$$

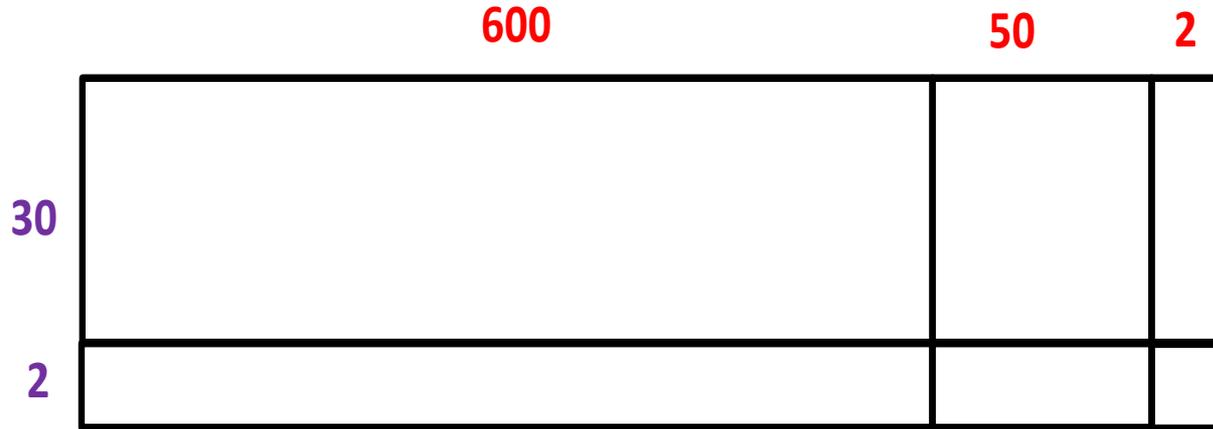
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Step 3: Since **652** is decomposed into three parts. Divide the longer side or the length into three parts. Write **600**, **50** and **3** over the divided parts.



Multiplying Multi-Digit Whole Numbers

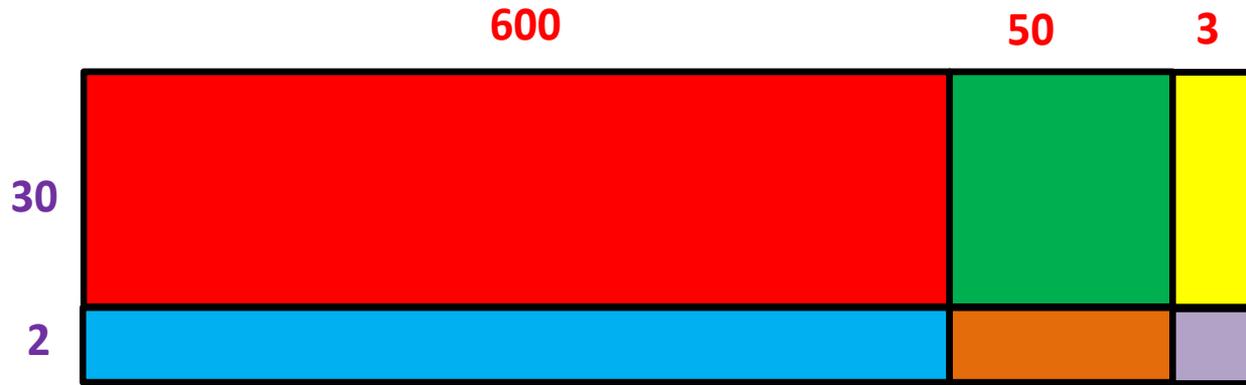
Step 4: Since **32** is decomposed into two parts. Divide the width into two parts. Write **30** and **2** over the divided parts. Label the parts.



Multiplying Multi-Digit Whole Numbers

Step 5:

Find the area of each rectangle. Let's color each rectangle differently and complete the table with its corresponding area.



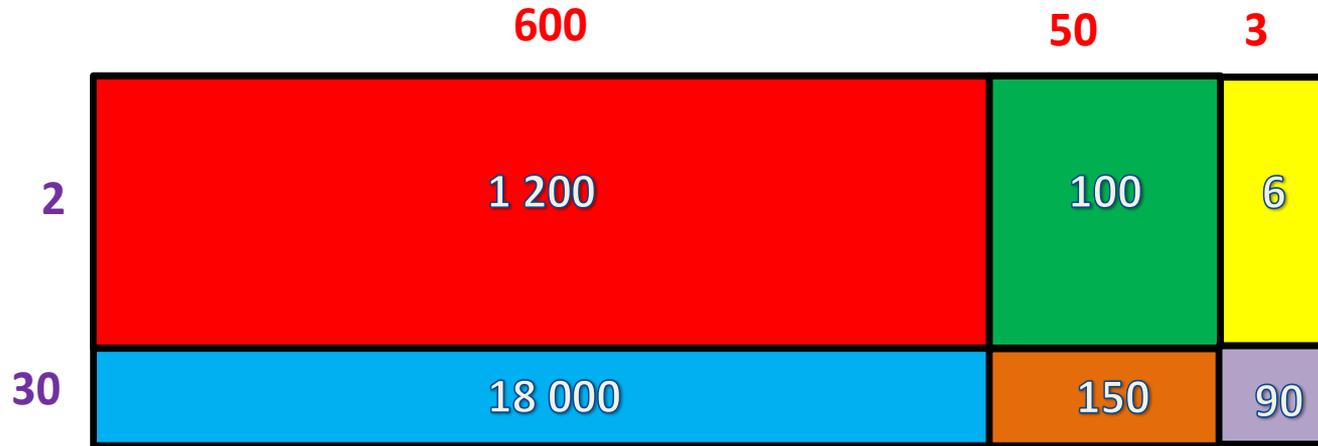
Multiplying Multi-Digit Whole Numbers

Step 5: Find the area of each rectangle. Let's color each rectangle differently and complete the table with its corresponding area.

| Rectangle | Dimensions | | Area of the Rectangle |
|-----------|------------|-------|-----------------------|
| | Length | Width | |
| | 600 | 30 | 18 000 |
| | 50 | 30 | 150 |
| | 3 | 30 | 90 |
| | 600 | 2 | 1 200 |
| | 50 | 2 | 100 |
| | 3 | 2 | 6 |

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Step 6: Write the product inside the corresponding rectangles.



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Step 7: Add all the area of the smaller rectangles to find the total area of the original rectangle.

| Rectangle | Dimensions | | Area of the Rectangle |
|--------------------------------------|------------|-------|-----------------------|
| | Length | Width | |
| | 600 | 30 | 18 000 |
| | 50 | 30 | 1 500 |
| | 3 | 30 | 90 |
| | 600 | 2 | 1 200 |
| | 50 | 2 | 100 |
| | 3 | 2 | 6 |
| Total area of the original rectangle | | | 20 896 |

Therefore, the product of 653 and 32 is **20 896!!!**

Multiplying Multi-Digit Whole Numbers

Sample Problem 1:

Find the product of 516 and 24 by drawing an area model.

Solution:

| | | | |
|----|--------|-----|-----|
| | 500 | 10 | 6 |
| 4 | 2 000 | 40 | 24 |
| 20 | 10 000 | 200 | 120 |

$$10\ 000 + 2\ 000 + 200 + 120 + 40 + 24 = 12\ 384$$

Therefore, $516 \times 24 = 12\ 384$

Multiplying Multi-Digit Whole Numbers

Steps in Multiplying Multi-Digit Numbers Using Partial Products

Example: Find the product of 612 and 15.

Step 1: Decompose each factor.

$$612 = 600 + 10 + 2$$

and

$$15 = 10 + 5$$

Multiplying Multi-Digit Whole Numbers

So...

$$\begin{array}{c} 612 \\ \swarrow \\ \boxed{600 + 10 + 2} \end{array}$$

x

$$\begin{array}{c} 15 \\ \swarrow \\ \boxed{10 + 5} \end{array}$$

x

Multiplying Multi-Digit Whole Numbers

Step 2: Multiply the 600 to each of the decomposed values of 15.

$$\textcircled{600} + 10 + 2 \quad \times \quad \textcircled{10 + 5}$$

$$600 \times 10 = 6000$$

$$600 \times 5 = 3000$$

Multiplying Multi-Digit Whole Numbers

Step 3: Multiply the 10 to each of the decomposed values of 15.

$$600 + 10 + 2 \quad \times \quad 10 + 5$$

$$600 \times 10 = 6000$$

$$600 \times 5 = 3000$$

$$10 \times 10 = 100$$

$$10 \times 5 = 50$$

Multiplying Multi-Digit Whole Numbers

Step 4: Multiply the 2 to each of the decomposed values of 15.

$$600 + 10 + 2 \times 10 + 5$$

$$600 \times 10 = 6\,000$$

$$600 \times 5 = 3\,000$$

$$10 \times 10 = 100$$

$$10 \times 5 = 50$$

$$2 \times 10 = 20$$

$$2 \times 5 = 10$$

6000, 3000, 100, 50,
20, and 10 are the
partial products of:

$$612 \times 15$$

Multiplying Multi-Digit Whole Numbers

Step 5: Add all the partial products of 612×15 .

$$6\ 000 + 3\ 000 + 100 + 50 + 20 + 10 = 9\ 180$$

Therefore, $612 \times 15 = 9\ 180$.

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Sample Problem 2:

Find the product of 453 and 72 using partial products.

Solution:

$$\underline{400 + 50 + 3} \times \underline{70 + 2}$$

$$400 \times 70 = 28\,000$$

$$400 \times 2 = 800$$

$$50 \times 70 = 3\,500$$

$$50 \times 2 = 100$$

$$3 \times 70 = 210$$

$$3 \times 2 = 6$$

$$28\,000 + 800 + 3\,500 + 100 + 210 + 6 = 32\,616$$

$$\text{Therefore, } 453 \times 72 = 32\,616$$

Standard Algorithm



What is "Standard Algorithm"?

When "**standard algorithm**" is defined separately, "standard" refers to something that is usual or common, while "algorithm" is a process or a set of rules to be followed in solving different types of operations.

Standard Algorithm



Combined, **standard algorithm** means the usual or common way of solving problems, such as multiplication, following a set of rules or steps. Here, you will fluently learn how to multiply multi-digit numbers using the standard algorithm.

Standard Algorithm for Multiplication

Just like **Addition** and **Subtraction**, the "**Standard Algorithm**" is also used in **Multiplication**. So long as you follow each step properly, rest assured that correct answers are obtained.



Standard Algorithm for Multiplication

Imagine you're trying to bake the yummiest chocolate cake ever! You are actually doing the same steps over and over again, very much the same in using standard algorithm for addition and subtraction (including all other operations).



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Multiplying Multi-Digit Whole Numbers

The Place Value and the Standard Algorithm

The concept of "place value" is very important in multiplying multi-digit numbers using the standard algorithm. Being very accurate when it comes to place values gives absolutely correct answers!

Multiplying Multi-Digit Whole Numbers

Steps in Multiplying Multi-Digit Numbers the Standard Algorithm

Example 1: Find the product of 376×47 .

Step 1: Align the factors vertically according to their place values.

$$\begin{array}{r} 376 \\ \times 47 \\ \hline \end{array}$$

Multiplying Multi-Digit Whole Numbers

Step 2: Multiply 7 to each digit of 375 starting with the ones digit. Don't forget to carry over the tens digit every time you multiply 7 to each digit of 375.

$$\begin{array}{r} 54 \\ 376 \\ \times 47 \\ \hline 2632 \end{array}$$

Multiplying Multi-Digit Whole Numbers

Step 3: Multiply 40 to each digit of 376 starting with the ones digit.

Why 40? Remember that in **47**, "4" is in the tens place... thus it has a value of "40".

$$\begin{array}{r} 32 \\ 376 \\ \times 47 \\ \hline 2625 \\ 15040 \end{array}$$



Adding "zero" means that we are multiplying by tens.

If you are multiplying a value in the hundreds place, then 2 "zeros" are added, because we are multiplying by hundreds.

Multiplying Multi-Digit Whole Numbers

Step 4: Add the partial products to get the final product.

$$\begin{array}{r} 376 \\ \times 47 \\ \hline 2632 \\ +15040 \\ \hline 17672 \end{array}$$

Therefore, $376 \times 47 = 17\,672$.

Multiplying Multi-Digit Whole Numbers

Example 2: Find the product of $4\,316 \times 252$.

$$\begin{array}{r} 4\,316 \\ \times 252 \\ \hline 8\,632 \\ 21\,5800 \longrightarrow \text{tens} \\ + 8\,63200 \longrightarrow \text{hundreds} \\ \hline 1\,087\,632 \end{array}$$

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Instead of "zeros" you can leave the zeros "blank" as well.

$$\begin{array}{r} 4316 \\ \times 252 \\ \hline 8632 \\ 215800 \rightarrow \text{tens} \\ + 863200 \rightarrow \text{hundreds} \\ \hline 1087632 \end{array}$$

$$\begin{array}{r} 4316 \\ \times 252 \\ \hline 8632 \\ 21580 \rightarrow \text{tens} \\ + 8632 \rightarrow \text{hundreds} \\ \hline 1087632 \end{array}$$

Multiplying Multi-Digit Whole Numbers

Sample Problem 3:

Find the product of 7 189 and 53 using the standard algorithm.

Solution:

$$\begin{array}{r} 7189 \\ \times 53 \\ \hline 21567 \\ + 35945 \\ \hline 381017 \end{array}$$

Multiplying Multi-Digit Whole Numbers

Multiplication of Multi-Digit Whole Numbers Word Problems

It is a known fact that Mathematics is a part of our daily lives. Whether we like it or not, we add, subtract, multiply and divide EVERYDAY... and we are quite not conscious that we actually do it!

Now that you know how to multiply multi-digit whole numbers using the standard algorithm... it's high time that you apply what you learned in solving word problems.

Multiplying Multi-Digit Whole Numbers

Example:

Sam bought 105 bikes for his rent-a-bike shop at \$637 each. How much did Sam spend for his bikes?



Solution:

$$\begin{array}{r} 105 \\ \times 637 \\ \hline 735 \\ 3150 \\ + 63000 \\ \hline 66885 \text{ bikes} \end{array}$$

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Sample Problem 4:

A concert will be held at a stadium with a capacity of 1584 people. If each ticket costs \$45, how much will the organizers earn if all tickets are sold?

Solution:

$$\begin{array}{r} 1584 \\ \times 45 \\ \hline 7920 \\ + 63360 \\ \hline \$71280 \end{array}$$